

Schedulability Analysis of Adaptive Variable-Rate Tasks with Dynamic Switching Speeds



Chao Peng¹, Yecheng Zhao², **Haibo Zeng**²

¹National University of Defense Technology, China

²Virginia Tech, USA





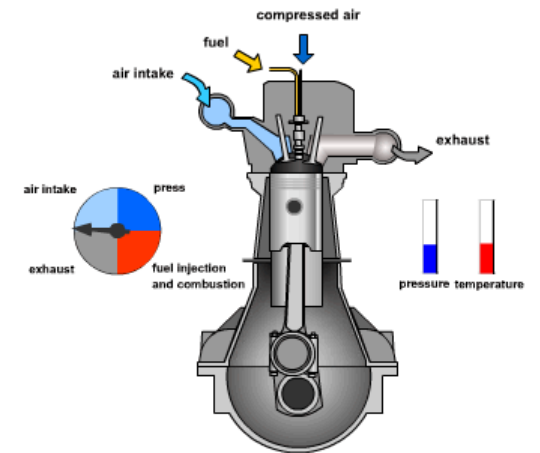
Outline

- System Model: dAVR tasks
 - Motivated by the opportunity to optimize engine operation at runtime
- Schedulability Analysis
 - Partitioning speed space (safe but pessimistic)
 - Partitioning release time space (exact)
- Experimental Evaluation
 - Typically 10%-26% better accuracy than transforming to sAVR tasks

AVR Tasks

Adaptive Variable-Rate (AVR) tasks

- Different control strategies at different engine rotation speed intervals
- Tradeoff between control performance and CPU workload

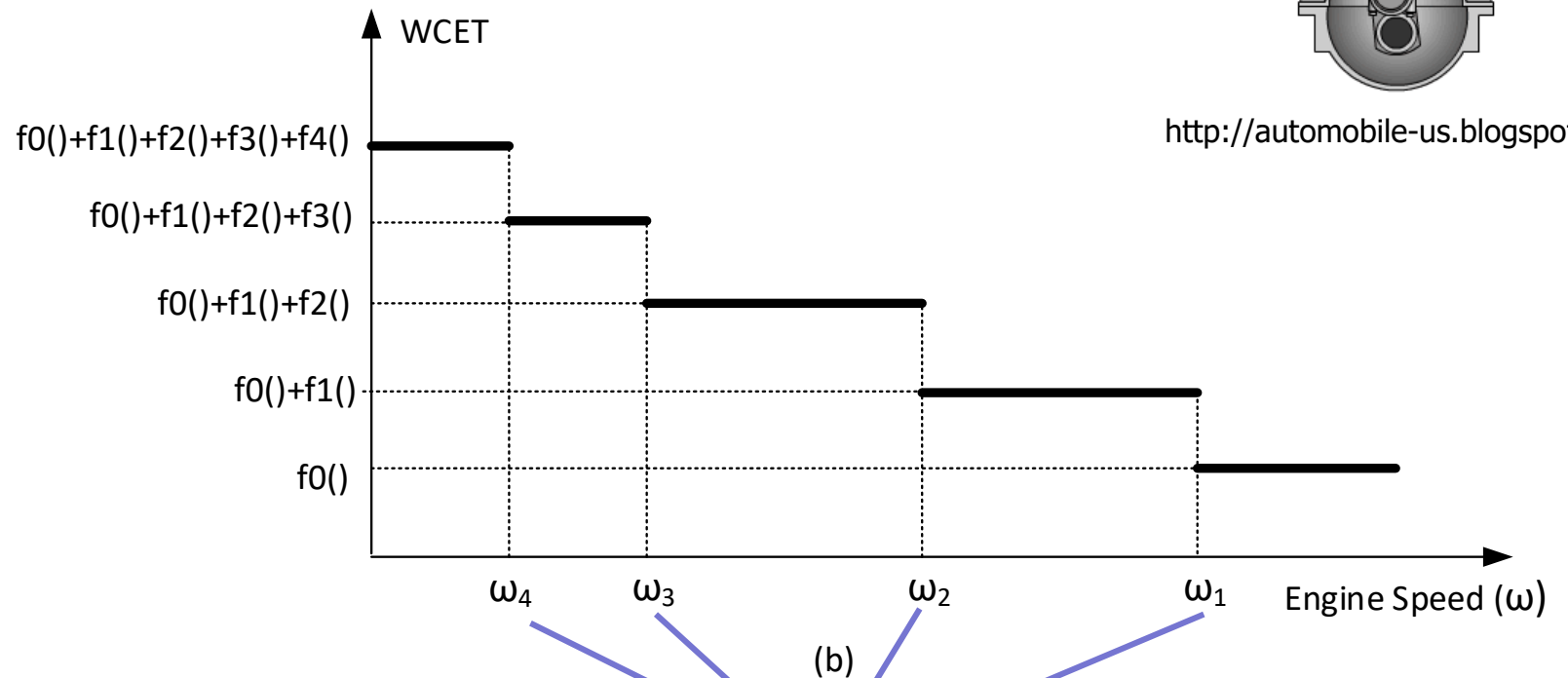


<http://automobile-us.blogspot.com>

```
#define ω4 1000
#define ω3 2000
#define ω2 4000
#define ω1 6000

task EC_task {
    ω = read_engine_speed();
    f0();
    if (ω ≤ ω1)    f1();
    if (ω ≤ ω2)    f2();
    if (ω ≤ ω3)    f3();
    if (ω ≤ ω4)    f4();
}
```

(a) [1]

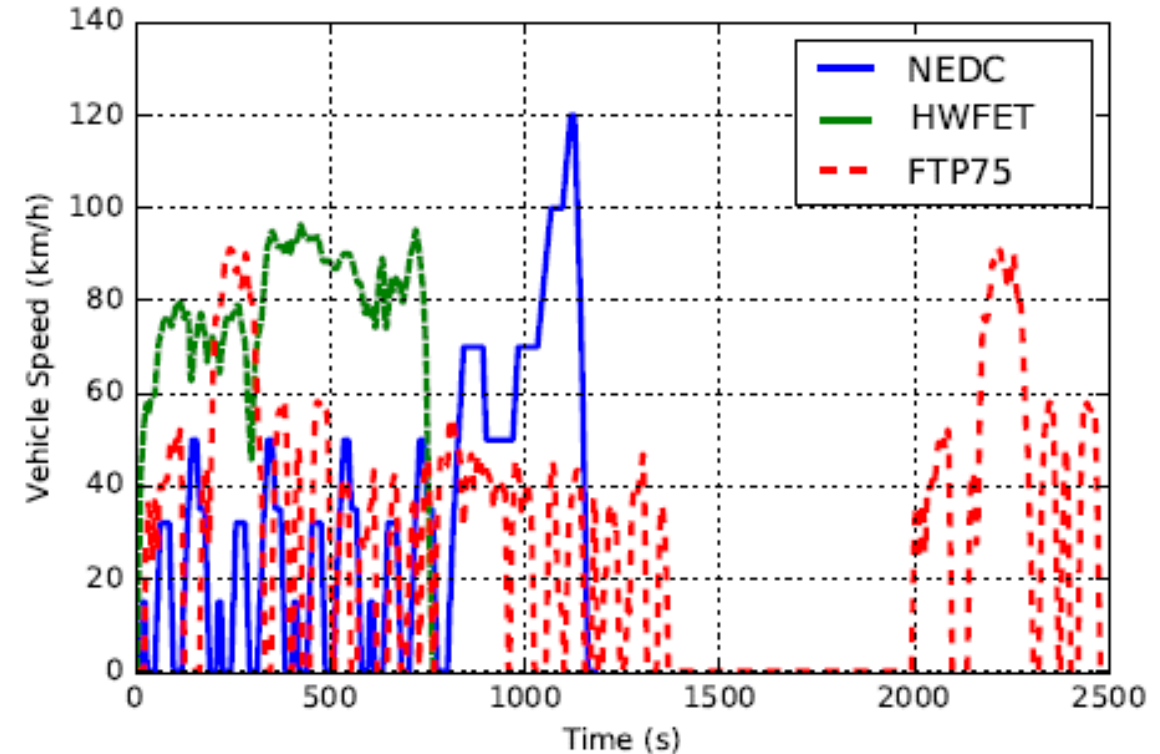


[1] D. Buttle, "Keynote speech: Real-time in the prime-time," in ECRTS 2012.

switching speeds **fixed at design time**

Motivation

- Suboptimal with static switching speeds
 - Difference among driving cycles
 - Variations within the same driving cycle
- Data available through connected and Automated Vehicles
 - Access to valuable information by using
 - Various sensing: camera, radar, lidar, ...
 - Communication: V2V, V2I, ...
 - Opportunities to improve vehicle operation
 - Engine control (including **switching speeds**)





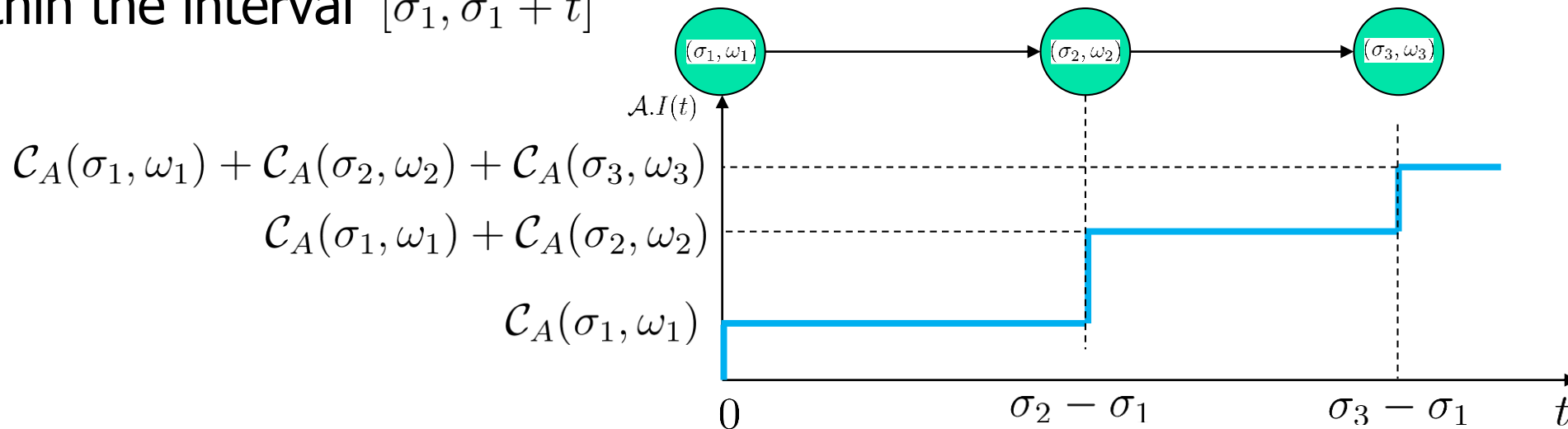
System Model

- Current approaches: static AVR (sAVR) tasks
 - the WCET of a job is a function of the engine speed
- Our proposal: dynamic AVR (dAVR) tasks
 - Reconfigured switching speeds at $\gamma_1, \gamma_2, \dots$
 - the WCET of a job is a function of the engine speed **and release time**

$$C_i(t, \omega) = C_{i,k}^m \quad \text{if } t \in [\gamma_k, \gamma_{k+1}) \wedge \omega \in (\omega_{i,k}^{m-1}, \omega_{i,k}^m]$$

Schedulability Analysis of Periodic Tasks

- AVR job = (release time, engine speed at release time)
- AVR job sequence $\mathcal{A} = [(\sigma_1, \omega_1), \dots, (\sigma_n, \omega_n)]$
- Interference function of AVR job sequence: the cumulative execution request within the interval $[\sigma_1, \sigma_1 + t]$



- Response time of periodic task τ_i interfered by AVR task τ_A^*

$$R(\tau_i, \tau_A^*) = \max_{\mathcal{A} \in \tau_A^*} R(\tau_i, \mathcal{A}), \text{ where}$$

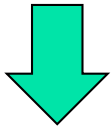
$$R(\tau_i, \mathcal{A}) = \min_{t > 0} \left\{ t \mid C_i + \sum_{\tau_j \in hp(i)} \left\lceil \frac{t}{T_j} \right\rceil C_j + \mathcal{A}.I(t) \leq t \right\}$$

Infinitely many \mathcal{A} due to continuous spaces of both release time and engine speed

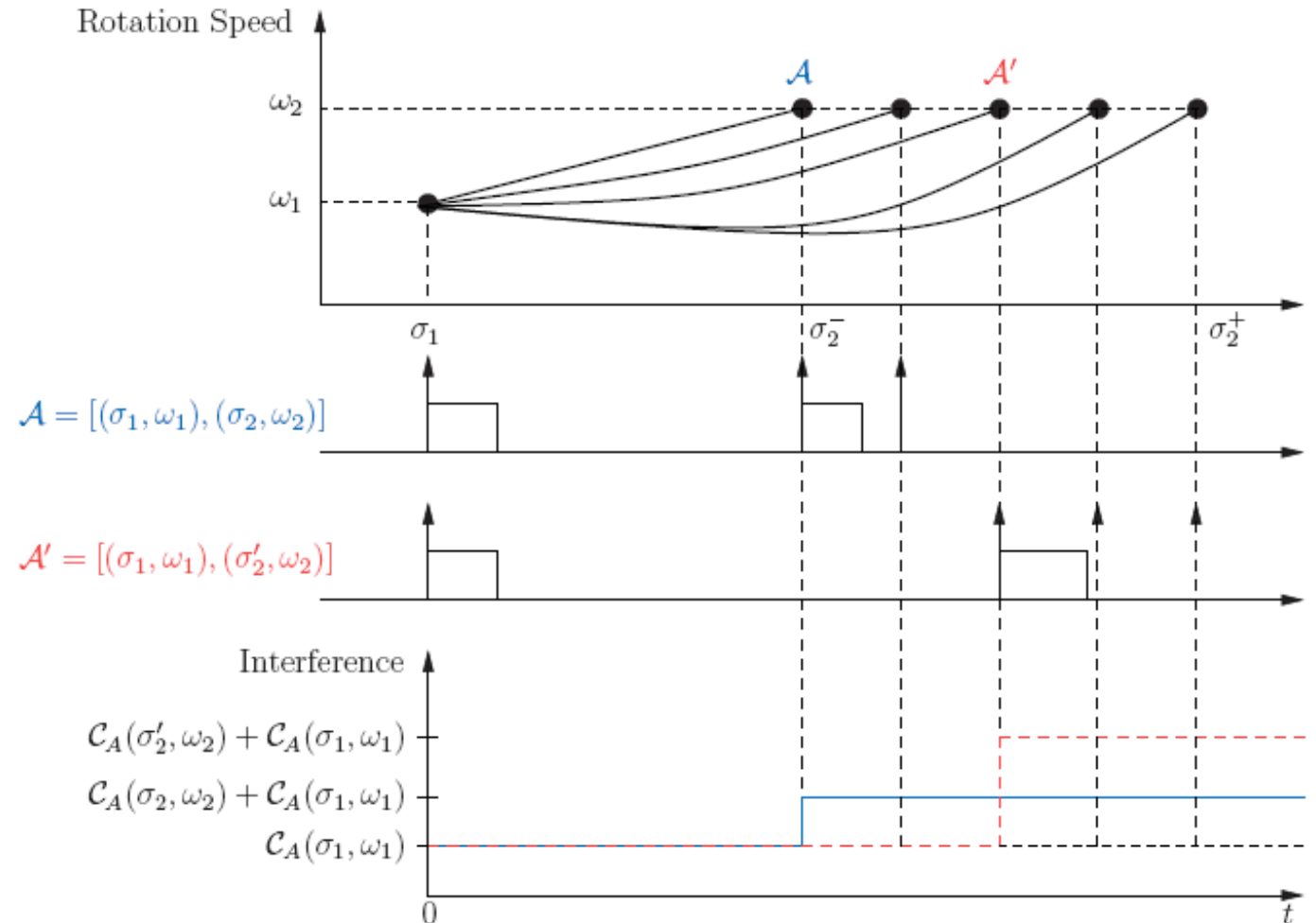
Difference between sAVR task and dAVR task

- Many analysis techniques for sAVR tasks are not applicable to dAVR

It is unsafe to only consider the minimum inter-release time between two consecutive jobs for dAVR tasks

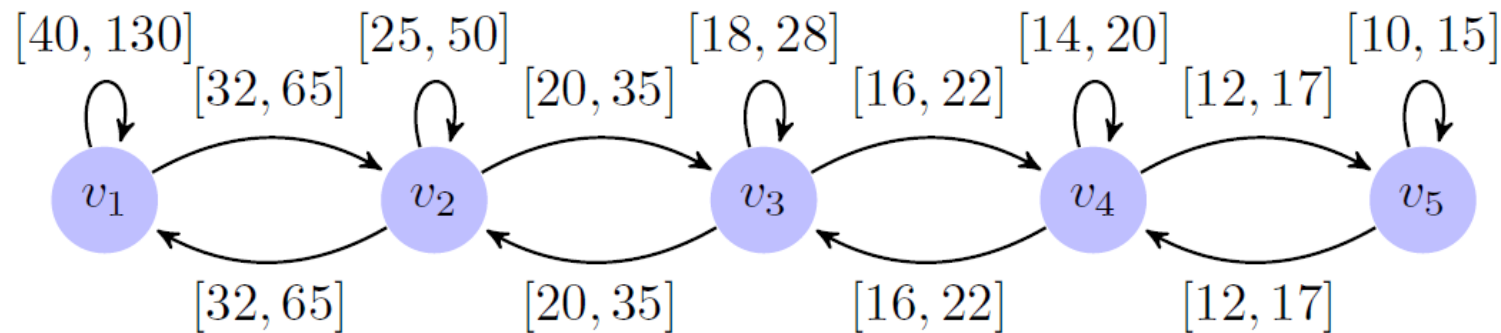


Necessary to keep the information on the minimum and **maximum** inter-release times between two consecutive jobs



Dynamic Digraph Real-Time (dDRT) Task Model

- Vertices represent a speed partition
 - Each vertex represents a separate speed interval
 - Also desirable to have WCET of each vertex only depends on the release time (but not the speed)
- An edge (v_i, v_j) is added if possible to release two consecutive jobs of type v_i and v_j respectively
 - Labeling it with the minimum and maximum inter-release times



dAVR to dDRT Transformation

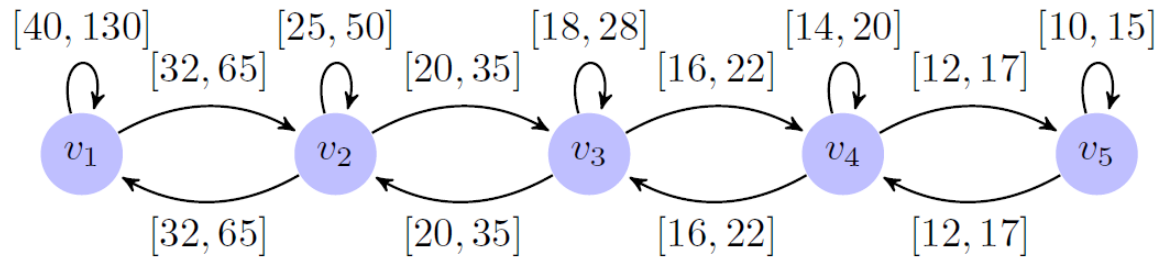
dAVR

Time Interval (ms)	Execution Modes					
$[\gamma_1, \gamma_2) = [0, 100)$	$\mathcal{M}_{i,1}$	m -th mode	1	2	3	
		$\omega_{i,1}^m$ (rpm)	2500	4500	6500	
		$C_{i,1}^m$ (μs)	600	400	200	
$[\gamma_2, \gamma_3) = [100, 200)$	$\mathcal{M}_{i,2}$	m -th mode	1	2	3	4
		$\omega_{i,2}^m$ (rpm)	1500	2500	4500	6500
		$C_{i,2}^m$ (μs)	600	400	300	200
$[\gamma_3, \gamma_4) = [200, +\infty)$	$\mathcal{M}_{i,3}$	m -th mode	1	2		
		$\omega_{i,3}^m$ (rpm)	3500	6500		
		$C_{i,3}^m$ (μs)	600	300		

Speed partition

$\{ [500, 1500], [1500, 2500], [2500, 3500], [3500, 4500], [4500, 6500] \}$

dDRT



v_1 represents speed interval $[500, 1500]$
 v_2 represents speed interval $[1500, 2500]$
 v_3 represents speed interval $[2500, 3500]$
 v_4 represents speed interval $[3500, 4500]$
 v_5 represents speed interval $[4500, 6500]$

WCET
function

Time Interval (ms)	WCET (μs)				
	v_1	v_2	v_3	v_4	v_5
$[\gamma_1, \gamma_2) = [0, 100)$	600	600	400	400	200
$[\gamma_2, \gamma_3) = [100, 200)$	600	400	300	300	200
$[\gamma_3, \gamma_4) = [200, +\infty)$	600	600	600	300	300

Schedulability Analysis based on Transformed dDRT

- Response time analysis based on the transformed dDRT τ_D^*
 - dDRT job = (release time, vertex)
 - dDRT job sequence $\mathcal{D} = [(\pi_1, \nu_1), \dots, (\pi_n, \nu_n)]$
 - Interference function of dDRT job sequence $\mathcal{D}.I(t)$
 - Response time of periodic task τ_i interfered by dDRT task τ_D^*

$$R(\tau_i, \tau_D^*) = \max_{\mathcal{D} \in \tau_D^*} R(\tau_i, \mathcal{D}), \quad \text{where}$$

$$R(\tau_i, \mathcal{D}) = \min_{t > 0} \left\{ t \mid C_i + \sum_{\tau_j \in hp(i)} \left\lceil \frac{t}{T_j} \right\rceil C_j + \mathcal{D}.I(t) \leq t \right\}$$



Properties of the Transformation

■ Safety

- Intuition: Each vertex presents an interval of engine speeds. Thus, for any dAVR job sequence \mathcal{A} , we can always find a dDRT job sequence \mathcal{D} such that they have the same interference function.

■ Pessimism

- For engines with maximum speed $\omega^{\max} > \omega^t$ where ω^t depends on the maximum acceleration/deceleration, the analysis is pessimistic
- Typical engines have $\omega^{\max} > 5.79 \omega^t$

Remaining Difficulty for Analyzing dDRT Systems

- Impractical to directly adopt the following computing equation

$$R(\tau_i, \tau_D^*) = \max_{\mathcal{D} \in \tau_D^*} R(\tau_i, \mathcal{D}), \text{ where}$$

$$R(\tau_i, \mathcal{D}) = \min_{t > 0} \left\{ t \mid C_i + \sum_{\tau_j \in hp(i)} \left\lceil \frac{t}{T_j} \right\rceil C_j + \mathcal{D}.I(t) \leq t \right\}$$

Still infinitely many \mathcal{D}
due to continuous space
of release time

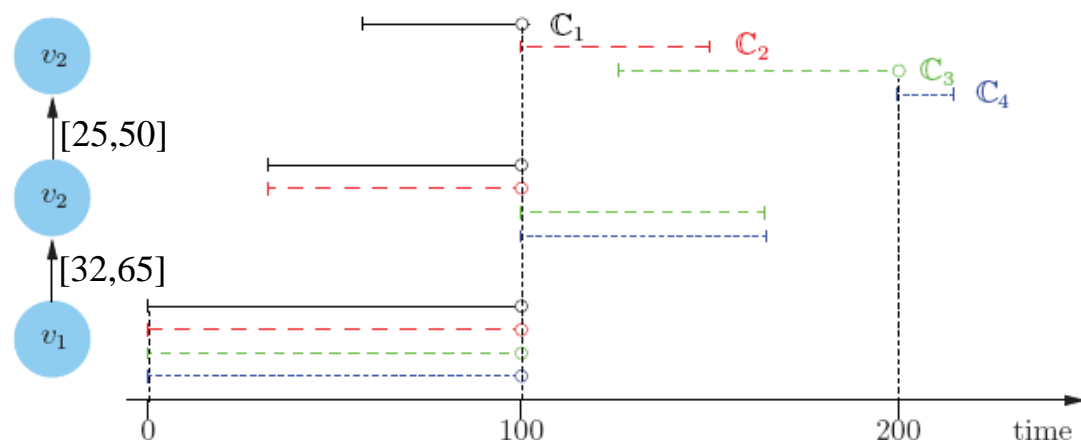
- Our Intuition:

- If two dDRT job sequences share the same sequence of job WCETs, then the one always with a shorter inter-release time will dominate the other in terms of their interference functions



Construction of Critical dDRT Job Sequence

- Example of constructing common-WCET dDRT job sequence sets



(a) Partitioning release time ranges by the reconfiguration times $\gamma_1 = 0, \gamma_2 = 100, \gamma_3 = 200$.

\mathbb{C}	(c_1^-, c_1^+, ν_1)	(c_2^-, c_2^+, ν_2)	(c_3^-, c_3^+, ν_3)
1	(0, 100, v_1)	(32, 100, v_2)	(57, 100, v_2)
2			(100, 150, v_2)
3		(100, 165, v_2)	(125, 200, v_2)
4			(200, 215, v_2)

(b) Resultant four common-WCET dDRT job sequence sets.

- Finding critical dDRT job sequences
 - Idea: the inter-release times are valid but also as tight as possible

```

1: procedure CONSTRUCTCRITICALJOBSEQUENCE( $\mathbb{C}$ )
2:    $\tilde{\mathbb{C}} \leftarrow [(\tilde{c}_1^-, \tilde{c}_1^+, \nu_1), \dots, (\tilde{c}_n^-, \tilde{c}_n^+, \nu_n)]$ ;
3:    $\tilde{c}_n^- \leftarrow c_n^-, \tilde{c}_n^+ \leftarrow c_n^+$ ;
4:   for  $l = n$  to 2 do // Backward Pass
5:      $\tilde{c}_{l-1}^- \leftarrow \max(\tilde{c}_l^- - p^{\max}(\nu_{l-1}, \nu_l), c_{l-1}^-)$ ;
6:      $\tilde{c}_{l-1}^+ \leftarrow \min(\tilde{c}_l^+ - p^{\min}(\nu_{l-1}, \nu_l), c_{l-1}^+)$ ;
7:    $\mathcal{D}^c \leftarrow [(\pi_1^c, \nu_1), \dots, (\pi_n^c, \nu_n)]$ ;
8:    $\pi_1^c \leftarrow \tilde{c}_1^+$ ;
9:   for  $l = 1$  to  $n - 1$  do // Forward Pass
10:     $\pi_{l+1}^c \leftarrow \max(\pi_l^c + p^{\min}(\nu_l, \nu_{l+1}), \tilde{c}_{l+1}^-)$ ;
11:  return  $\mathcal{D}^c$ ;

```

\mathbb{C}	Line 3		Lines 4–6				Line 8	Lines 9–10	
	\tilde{c}_3^-	\tilde{c}_3^+	\tilde{c}_2^-	\tilde{c}_2^+	\tilde{c}_1^-	\tilde{c}_1^+	π_1^c	π_2^c	π_3^c
1	57	100	32	75	0	43	43	75	100
2	100	150	50	100	0	68	68	100	125
3	125	200	100	165	35	100	100	132	157
4	200	215	150	165	85	100	100	150	200

contains invalid
job sequence

can't be tighter
due to validity



Experimental Setting

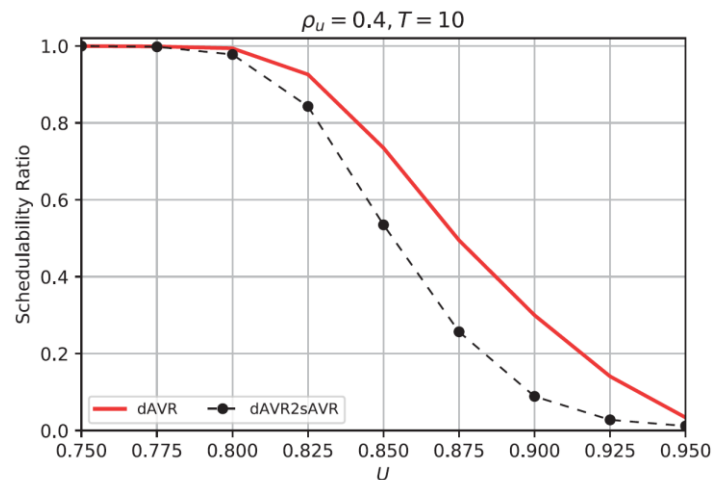
- Schedulability analysis methods
 - **dAVR**: our proposed approach
 - **dAVR2sAVR**: the sufficient-only analysis by transforming dAVR tasks to sAVR tasks and then apply the existing analysis on sAVR [1]
 - **UB**: the necessary-only analysis proposed in [2]
- Random task systems are generated following [1]
 - 20 Periodic tasks with constrained deadline:
 - period is randomly chosen from [3,100] ms
 - One AVR task: the execution modes are set as [1], with
 - Reconfiguration time interval = 500ms (typical driving cycle sample time)

[1] Biondi et al., "Response-time analysis for real-time tasks in engine control applications," in IEEE/ACM Conference on Cyber-Physical Systems, 2015.

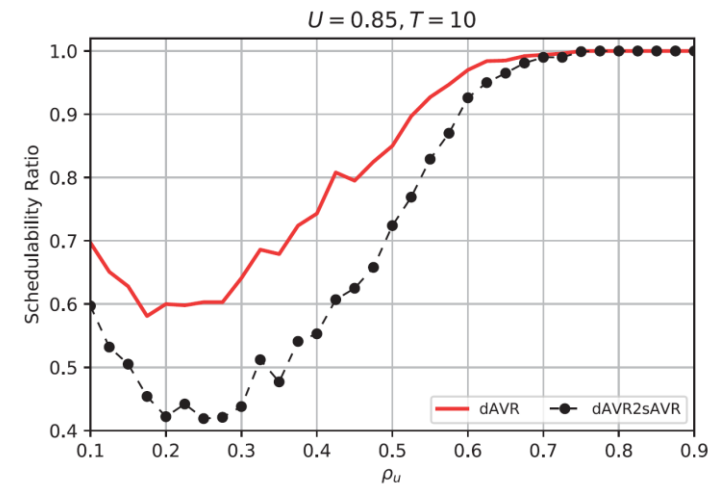
[2] Biondi et al., "Performance-driven design of engine control tasks," in IEEE/ACM Conference on Cyber-Physical Systems, 2016.

Experimental Results

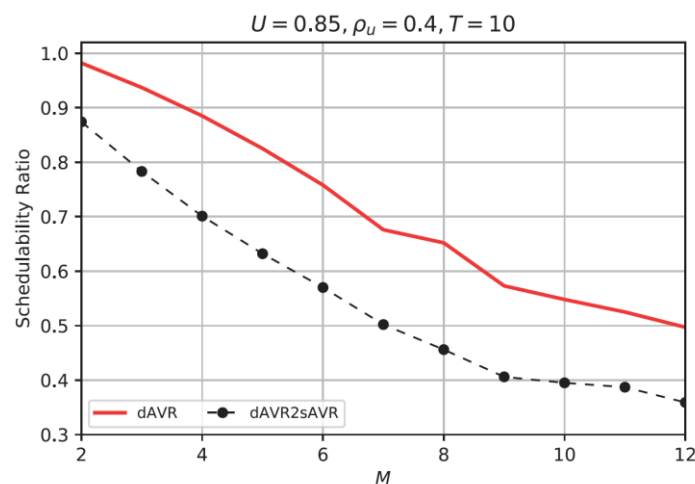
dAVR always has a **higher** analysis accuracy than dAVR2sAVR (typically 10%-26% in terms of schedulability ratio)



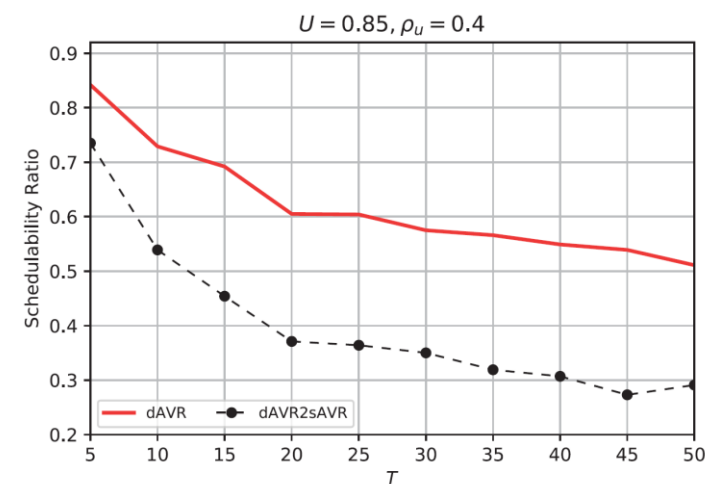
Schedulability ratio vs. system utilization U



Schedulability ratio vs. dAVR utilization fraction ρ_u



Schedulability ratio vs. number of modes M



Schedulability ratio vs. number of configurations T



Conclusion and Future Work

- Contributions:
 - Dynamic AVR task model that reconfigures the switching speeds at runtime
 - Response time analysis by partitioning
 - the speed space (sufficient-only)
 - release time space (exact)
- Typically 10%-26% more accurate than transforming it to static AVR
- Future work:
 - The approximation quality of speed partition
 - Optimization of switching speeds at runtime



Thank you!

Email: hbzeng@vt.edu